

# High Performance Computing

ADVANCED SCIENTIFIC COMPUTING

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SHORT LECTURE 12

## Terrestrial Systems & Climate

November 7<sup>th</sup>, 2017

Room TG-227



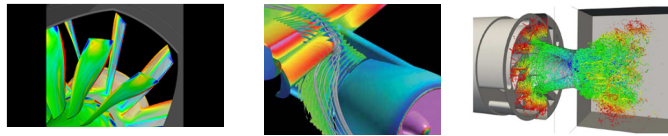
UNIVERSITY OF ICELAND  
SCHOOL OF ENGINEERING AND NATURAL SCIENCES

FACULTY OF INDUSTRIAL ENGINEERING,  
MECHANICAL ENGINEERING AND COMPUTER SCIENCE



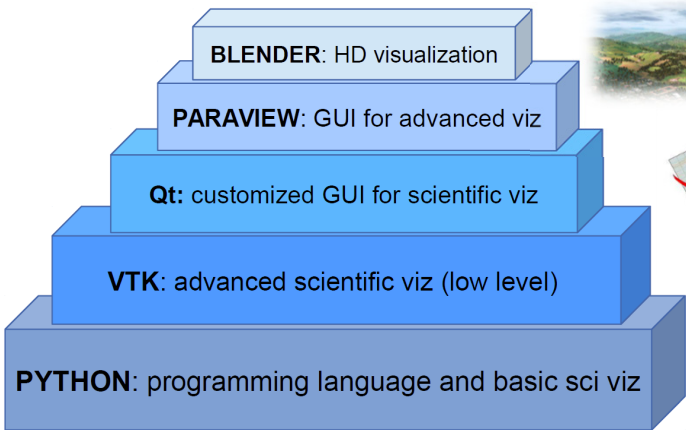
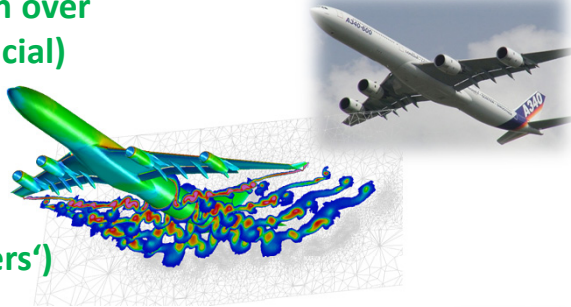
# Review of Lecture 11 – Scientific Visualization & Steering

## Many Visualization Methods



(visualization over time is crucial)

(‘a picture is worth 1000 words numbers’)



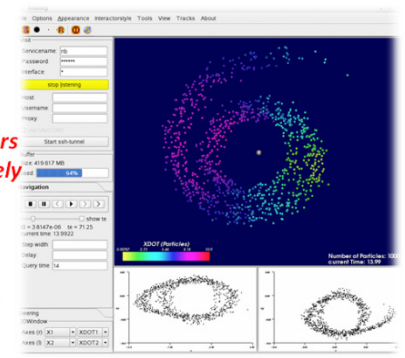
## Interactively Steer HPC Applications while executing

```
call flvisit_nbody2_steering_recv(
& VISITDPARM1,VISITDPARM2,VISITDPARM3,
& VISITDPARM4,VISITIPARM1,VISITIPARM2,...)
...
if(LVISIT_ACTIVE.eq.1) Then
VDISTANCE=VISITDPARM4
write(*,*) 'VISCON: VDISTANCE=',VDISTANCE
endif
...
IF(VISITDPARM2.gt.0) THEN
DTADJ = VISITDPARM2
END IF
IF(VISITDPARM3.gt.0) THEN
DELTAT = VISITDPARM3
END IF
...
CALL MPI_BCAST(DTADJ,1,MPI_DOUBLE_PRECISION,
0,& MPI_COMM_WORLD,ierr)
CALL MPI_BCAST(VISITDPARM3,1,
MPI_DOUBLE_PRECISION,0,& MPI_COMM_WORLD,...)
```

MPI

change parameters interactively

visualize status

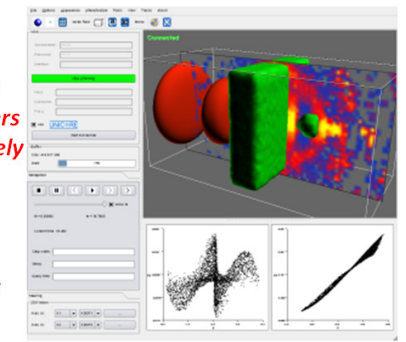


```
subroutine vis_control
...
integer :: isteer1=0,isteer2=0,isteer3=0,...
real*8 :: dsteer1,dsteer2,dsteer3,dsteer4
...
call flvisit_nbody2_check_conn(lvisit_active)
call flvisit_nbody2_steering_recv(dsteer1,...
...,dsteer3,dsteer4,...,isteer3,isteer4)
th_beam = dsteer1
r_beam = dsteer4
i_vis_max = max(isteer2,2)
i_vis_fields = max(isteer3,2)
...
call MPI_BCAST(th_beam,1,MPI_REAL,0,
MPI_COMM_WORLD,ierr)
...
```

MPI

change parameters interactively

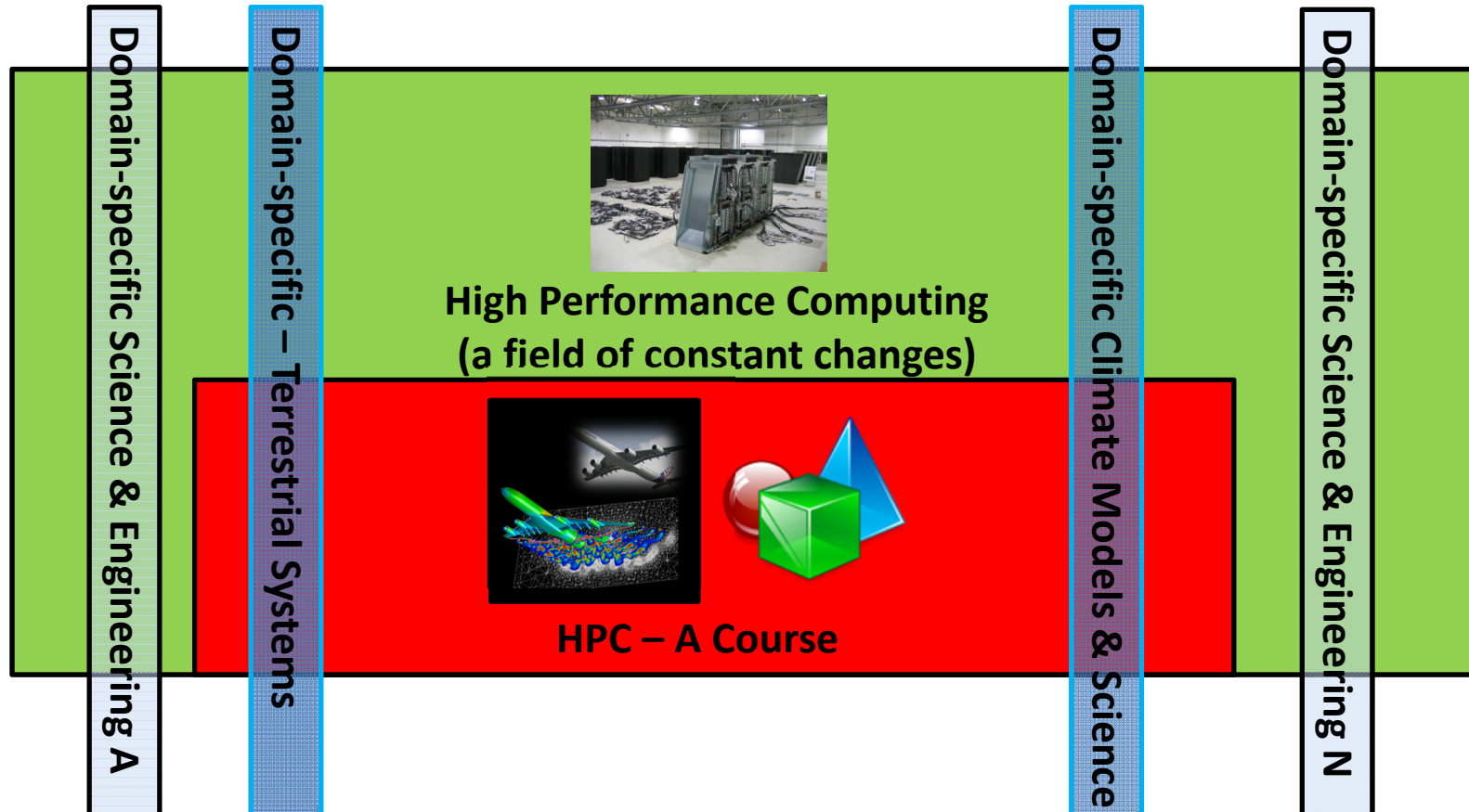
visualize status



modified from [1] CINECA – Scientific Visualization Training [2] M. Riedel et al., computational steering, 2007

# HPC-A[dvanced] Scientific Computing – Second Part

- Consists of techniques for programming large-scale HPC Systems
  - Approach: Get a broad understanding what HPC is and what can be done
  - Goal: Train general HPC techniques and **bits of domain-specific applications**



# Outline of the Course

1. High Performance Computing
  2. Parallelization Fundamentals
  3. Parallel Programming with MPI
  4. Advanced MPI Techniques
  5. Parallel Algorithms & Data Structures
  6. Parallel Programming with OpenMP
  7. Hybrid Programming & Patterns
  8. Debugging & Profiling Techniques
  9. Performance Optimization & Tools
  10. Scalable HPC Infrastructures & GPUs
  11. Scientific Visualization & Steering
  12. Terrestrial Systems & Climate
  13. Systems Biology & Bioinformatics
  14. Molecular Systems & Libraries
  15. Computational Fluid Dynamics
  16. Finite Elements Method
  17. Machine Learning & Data Mining
  18. Epilogue
- + additional practical lectures for our hands-on exercises in context

# Outline

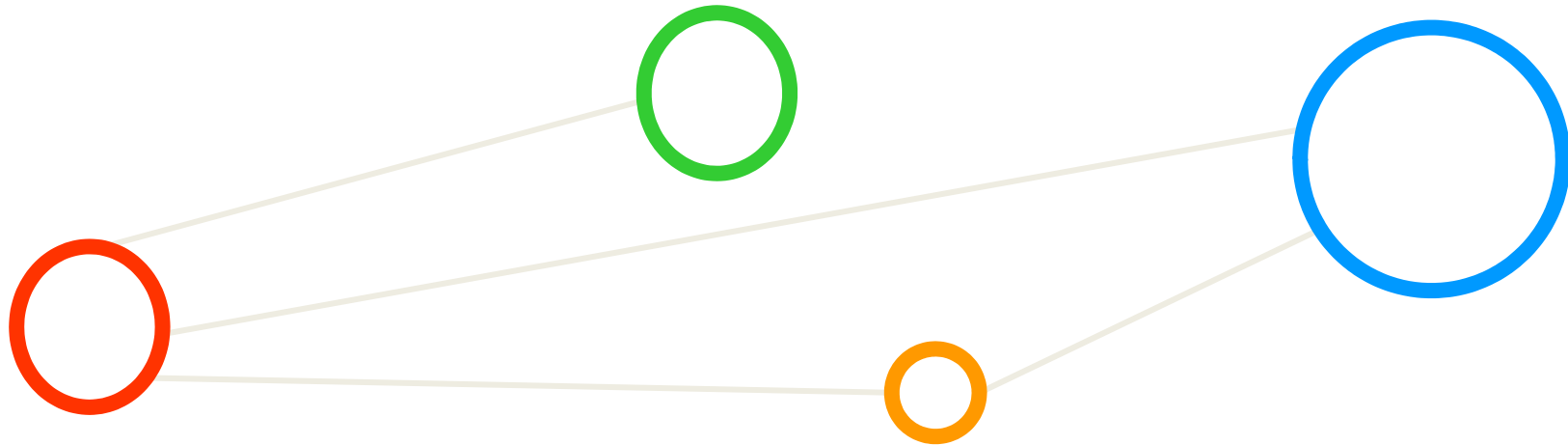
- Terrestrial Systems
  - Numerical Simulations
  - ParFlow Hydrology Model
  - CLM Land-Surface Model
  - COSMO Weather Model
  - Coupling Different Models
- Climate
  - Numerical Weather Prediction
  - Partial Differential Equations
  - WRF Model Application
  - WRF Parallel I/O & pNetCDF

➤ Short Lecture only shows subsets of libraries & applications in domains

Short Lecture 12 – Terrestrial Systems & Climate

- Promises from previous lecture(s):
- *Lecture 2:* Lecture 12 about Terrestrial Systems will provide more details on domain decomposition aspects
- *Lecture 2:* Lectures 12-17 will provide details on applied parallelization methods within parallel applications
- *Lecture 4:* Lectures 12-17 will provide parallel application examples that take advantage of the NetCDF
- *Lecture 5:* Lecture 12 will give in-depth details on parallel algorithms used in terrestrial systems and climate
- *Lecture 5:* Lectures 12-17 will provide more details on how NETCDF and HDF is used with application data
- *Lecture 5:* Lectures 12-17 will provide more details on complexities integrating technical & domain code
- *Lecture 7:* Lecture 12 will provide more HPC examples from terrestrial systems and climate simulations
- *Lecture 11:* Lecture 12-17 will provide scientific visualizations for different HPC application domain fields

# Terrestrial Systems

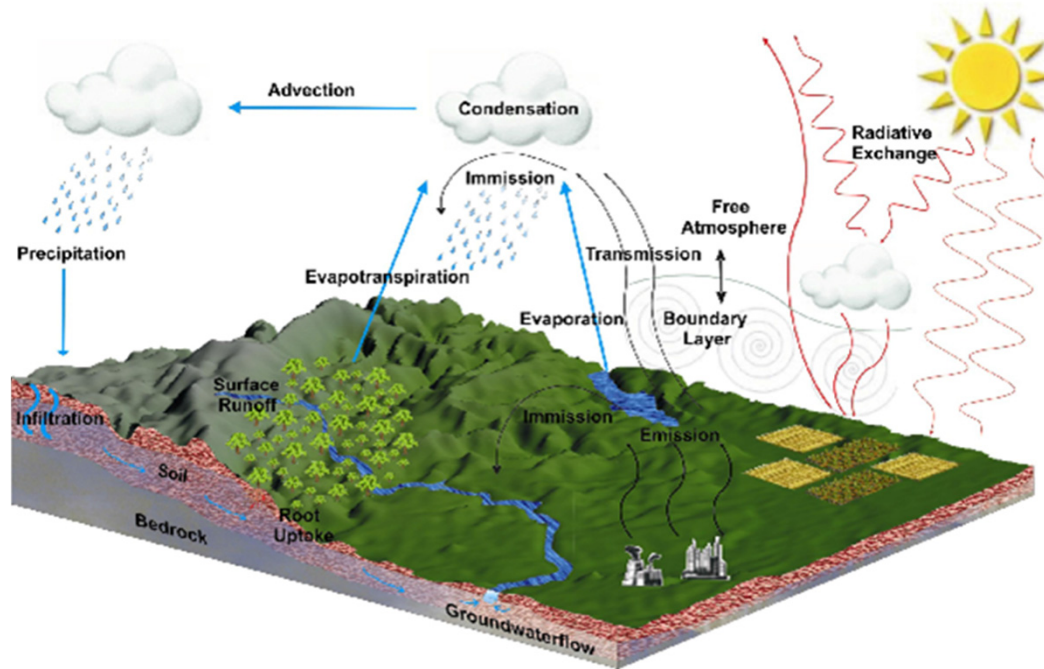


# Terrestrial Systems – Motivation

- Terrestrial systems represent a class of applications that perform numerical HPC simulations of variable complexity of terrestrial systems processes across different scales & regions

*modified from [3] SimLab Terrestrial Systems*

Physical system changes are accompanied by major state changes of land surfaces & ecosystems



State changes of land surfaces & ecosystems and services provided by them have multiple socioeconomic impacts

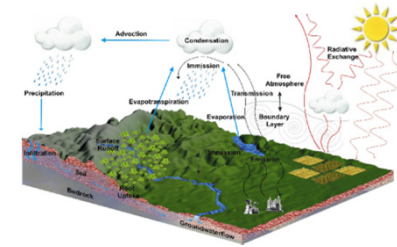
- Selected Motivations

- Understand global environmental change (e.g. climate) affecting terrestrial systems at all scales
- Increase understanding of many physical processes on earth (latin terra) that are still poorly understood
- Work towards better reproducibility of models

# Terrestrial Systems – Modelling Dynamical Systems

- Evolution in time (and space) is of interest

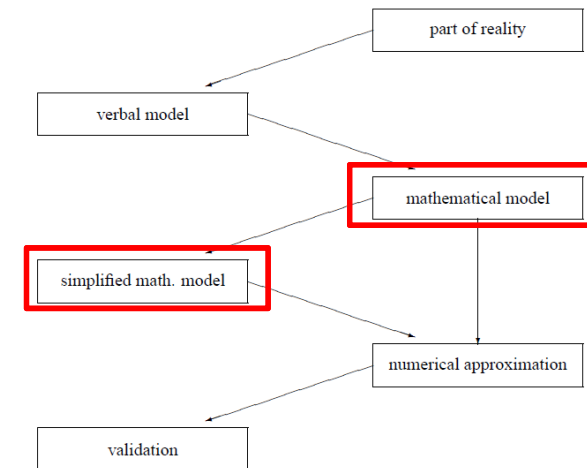
- Behavior of a whole ecosystem in time
- Dynamical systems:  
e.g. economic processes, movement of a fluid, ...
- (cf. Lecture 7 simple Jacobi example & heat equation)



[3] SimLab Terrestrial Systems

- How to model ‘evolution’ of a system

- A dynamical system consists of its state (e.g. input data) and a some ‘rules’
- Rules determine how the dynamic system will evolve over time
- Rules governing the evolution are ‘physical laws/equations for different system elements’



[4] Introduction to SC

- In order to investigate a real system’s behaviour by computing, a mathematical model is needed
- A dynamical system is some realistic system whose evolution in time is of interest



# Terrestrial Systems – Need for Numerical Methods in HPC

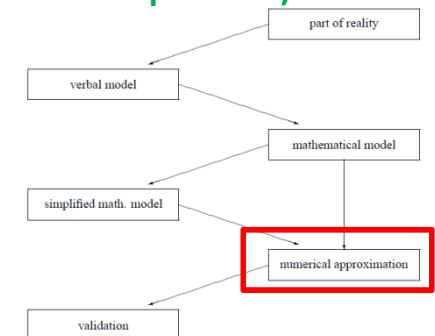
- Solving some mathematical problems & equations is too computational intensive → approximate
- Numerical methods are methods that obtain numerical approximation solutions to problems

[4] Introduction to SC

- Behaviour ‘governed by equations’ are computed
  - Nature is complex & interconnected: simplification
- Behaviour governed by ‘difference equations’
  - System state only change at discrete instants of time
  - System state ‘not change in time continuously’
- Behaviour governed by ‘differential equations’
  - System state evolves ‘continuously in time’
- Selected ‘scientific questions’ for simulations
  - Under what circumstances will a system evolve into an ‘equilibrium–state’ (state which does not change)
  - Under what circumstances will the system evolve into a ‘periodic state’ (states the system return to over time )

(solutions can be computed simply by applying definitions iteratively)

(harder to solve, e.g. initial value problem)



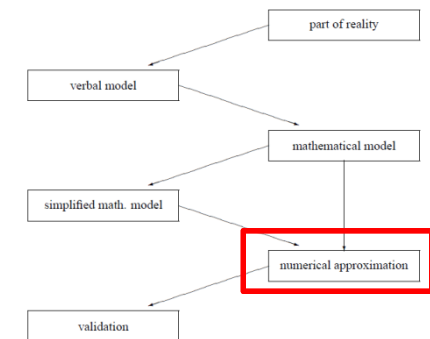
# Terrestrial Systems – Partial Differential Equations (PDEs)

- HPC models often use toolkits (e.g. PETSc) for Partial Differential Equations (PDEs) that are differential equations that contains unknown multivariable functions and their partial derivatives
- A general method in HPC modelling use parallel PDEs tools to approximate solutions to problems

*modified from [5] Wikipedia on 'Partial Differential Equation'*

- HPC simulation modelling
  - PDEs enable **rates of change** (of continuous variables)
  - PDEs used to formulate problems involving **functions of several variables**
  - PDEs describe a **wide variety of phenomena** (e.g. sound, heat, electrostatics, fluid flow, etc.)
  - PDEs model **multi-dimensional dynamical systems**
- Differences to '**ordinary differential equations**'
  - Ordinary differential equations deal with **functions of a single variable** and their derivatives
  - Ordinary differential equations model **one-dimensional dynamical system**

Solving those equations is often too complicated computationally expensive or impossible to analytically compute driving the need for numerical approximation

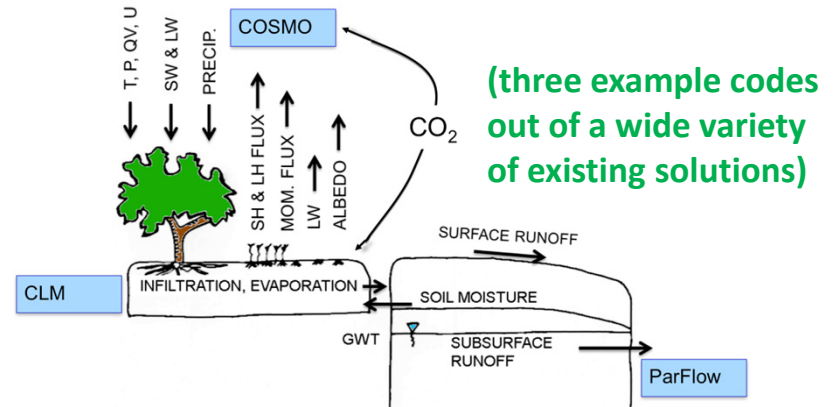


*[4] Introduction to SC*

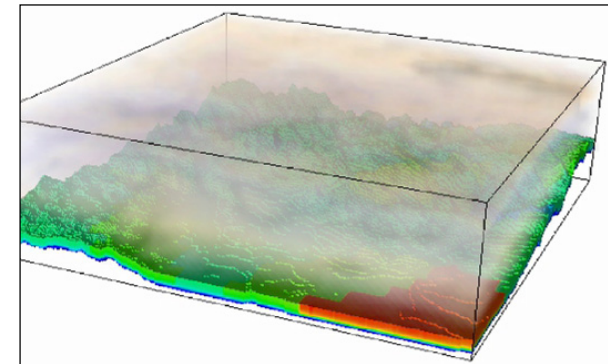
# Terrestrial Systems – Numerical HPC Simulations

- Numerical models & simulations

- Investigate multiple **terrestrial system processes** as a whole
- Enable **sustainable management** of terrestrial systems
- Simulate **complex, non-linear transport processes** of energy, mass and momentum
- Create **interactions and feedback mechanisms** between different compartments of the coupled **geo-ecosystem** (e.g. subsurface, land-surface, atmosphere, reservoirs, etc.)



[3] SimLab Terrestrial Systems

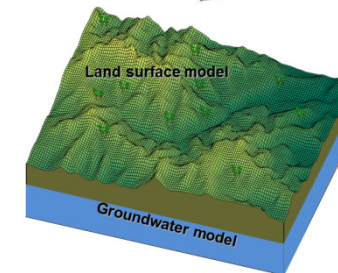
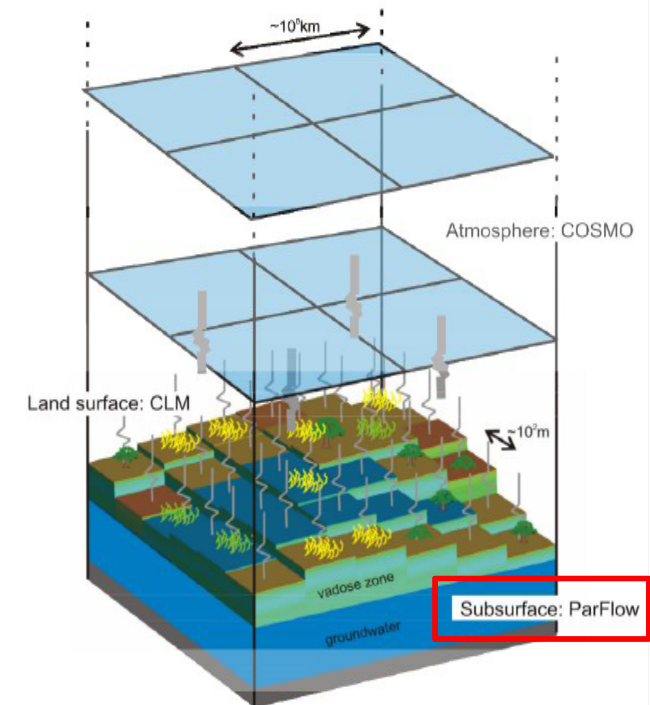


- **Varying scales:** multiple spatio-temporal scales and **high resolutions**
- Potentially long runtimes & use **'ensemble simulations'**

➤ **Lecture 13 provides more details on ensemble methods to estimate uncertainties in bio-systems**

# Terrestrial Systems – ParFlow Model Parallel Application (1)

- Modelling ‘hydrology’ processes
  - Parallel watershed flow model (ParFlow)
  - Simulate surface and subsurface fluid flow
  - Use in the assessment and management of groundwater and surface water
  - Investigate system physics and feedbacks
  - Understand interactions at a range of scales
  - Suitable for large scale & high resolution
- Parallel ‘numerical’ application
  - Developed over 10 years (aka stable code)
  - Offers advanced numerical solvers for massively parallel HPC systems



[6] R. Maxwell

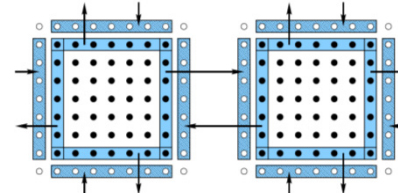
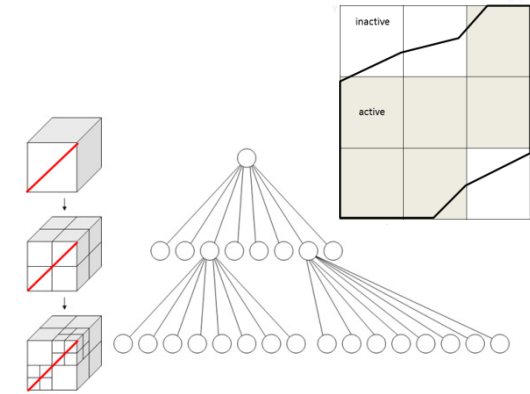
[7] ParFlow Web page

- ParFlow enables the parallel simulation of hydrology processes with (sub-)surface fluid flows

# Terrestrial Systems – ParFlow Model Parallel Application (2)

- Parallelization Techniques

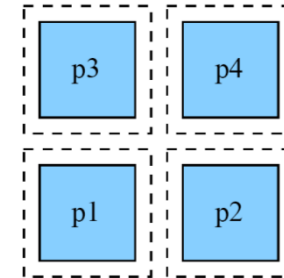
- 3D Grid **domain decomposition** (cf. Lecture 2)
- 3D code (use octree-space partitioning algorithm)
- Implements **hybrid programming** (cf. Lecture 7)
- Requirement of **‘halo regions’** for numerical equations (cf. Lecture 7)



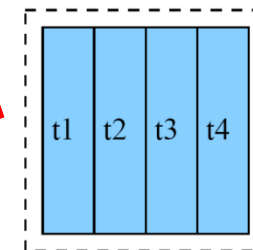
Distributed memory across the grid & halo updates

[6] HPC & ParFlow

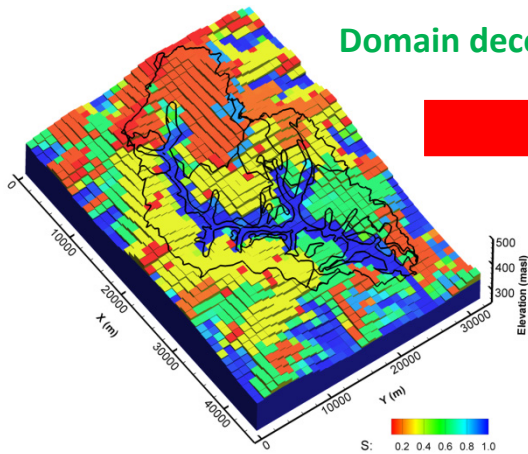
message-passing



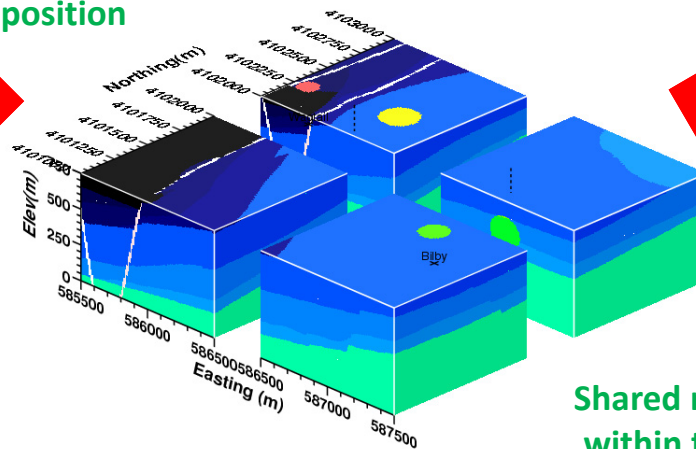
shared-memory



Shared memory within the grid



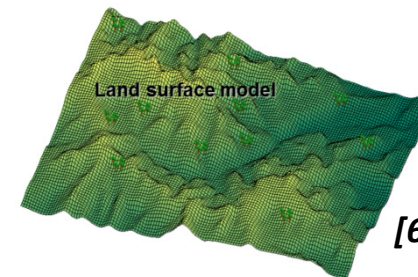
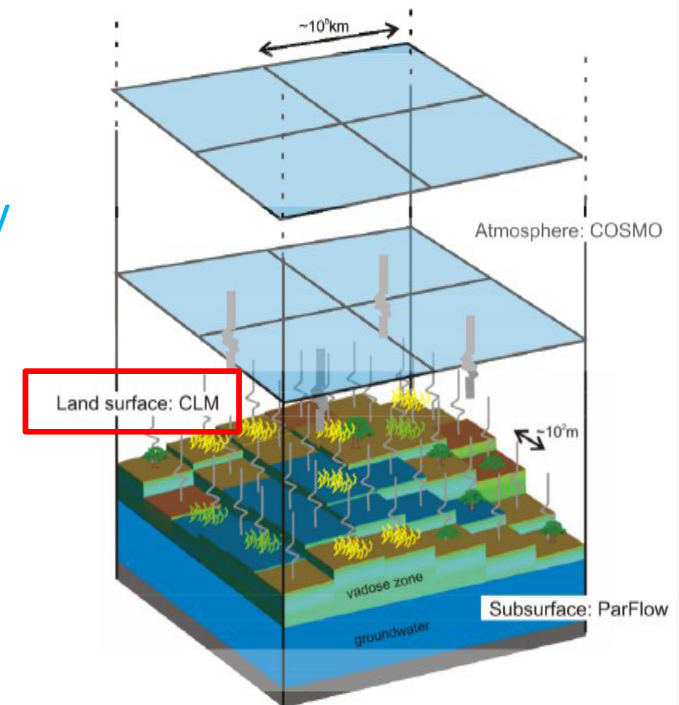
Domain decomposition



[7] ParFlow Web page

# Terrestrial Systems – CLM Model Parallel Application (1)

- Modelling 'land surface' processes
  - Community land model (CLM)
  - Simulates concepts of ecological climatology
  - Understand how natural & human changes in vegetation affect the climate
  - Examine physical, chemical, and biological processes that affect (or are affected by) climate across spatial / temporal scales
  - Investigate terrestrial ecosystems through their cycling of energy, water, chemical elements, and trace gases
  - Explore impact of terrestrial ecosystems as important determinants of climate



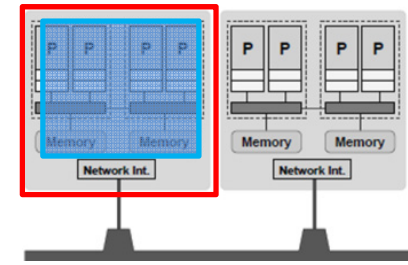
[6] R. Maxwell

[8] CLM Web page

- CLM enables the parallel simulation of land-surface with physical/chemical/biological processes

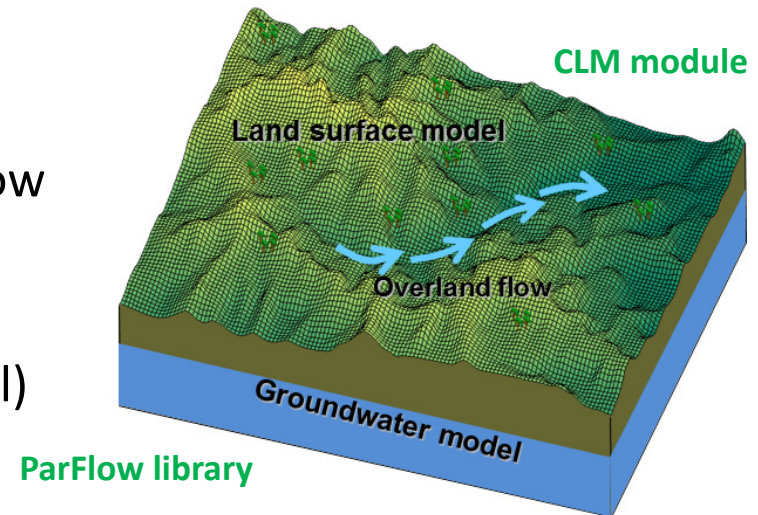
# Terrestrial Systems – CLM Model Parallel Application (2)

- Parallelization Techniques
  - Implements ‘hybrid programming’ (cf. Lecture 7)
  - OpenMP within a node (cf. Lecture 6)
  - MPI routines for parallelism across nodes (cf. Lecture 3)



[6] R. Maxwell

- Coupled as module
  - Code is often fully coupled with ParFlow
  - Coupling is performed in a way that CLM is incorporated into ParFlow as a module (full coupled, fully parallel)
  - E.g. flow of water on land-surface affects groundwater model



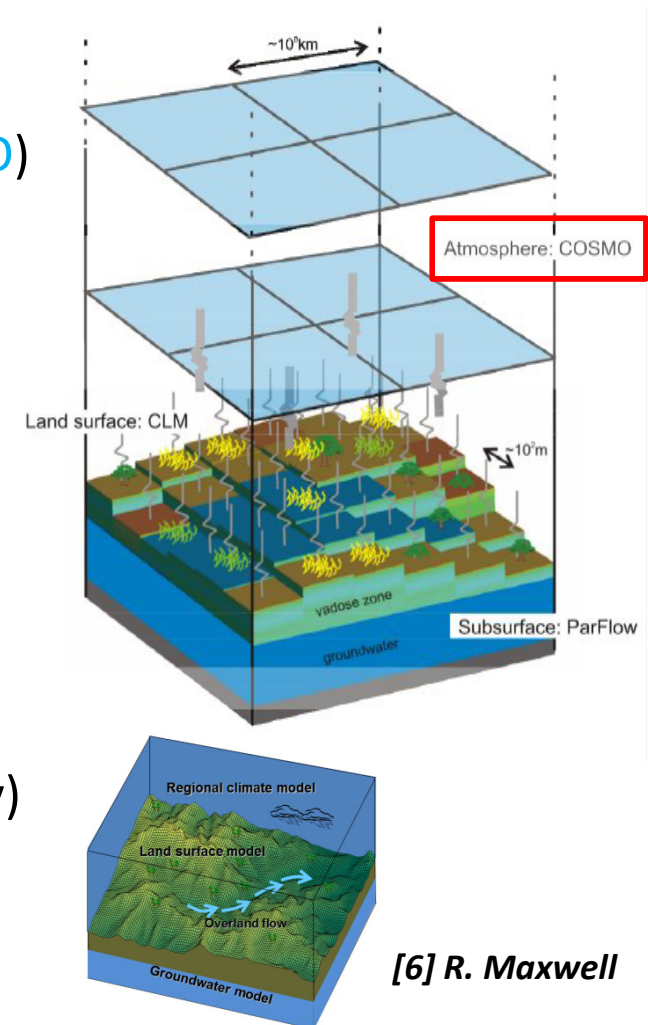
■ Coupling can be done using modules where one library is a module to another in one executable

# Terrestrial Systems – COSMO Model Parallel Application (1)

- Modelling ‘atmosphere’ processes
  - Consortium for Small-scale Modeling (**COSMO**)
  - Atmospheric model based on Fortran 90 & **numerical methods to simulate weather**
  - Use for non-hydrostatic limited-area (e.g. **regional atmospheric model**)
  - Use **a variety of physical processes** by parameterization schemes
  - Perform ‘**Data assimilation**’ from various observations (simulation alone not sufficient)
    - E.g. radiosonde (wind, temperature, humidity)
    - E.g. aircraft (wind, temperature)
    - E.g. wind profiler (wind)

[9] COSMO Web page

- **COSMO enables the parallel simulation of detailed regional atmospheric model processes**



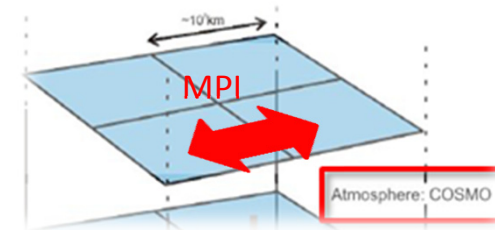
[6] R. Maxwell



# Terrestrial Systems – COSMO Model Parallel Application (2)

- Parallelization Techniques

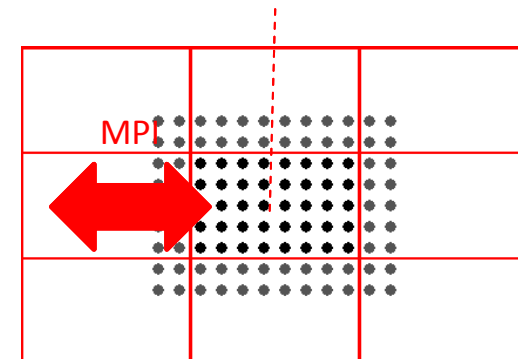
- Distributed memory using **MPI** (cf. Lecture 3)
- Two dimensional **domain decomposition** (cf. Lecture 2)
- Each processor gets a part of data (one subdomain)
- Solves model equations in parallel



- Use of ‘**halo technique**’ (cf. Lecture 7)

- 2 halo gridlines that belong to neighbor (configurable property)
- Different computing/solver schemes **require different halo lines** (2 or 3)
- Grid points belonging to the **halo are exchanged using MPI**

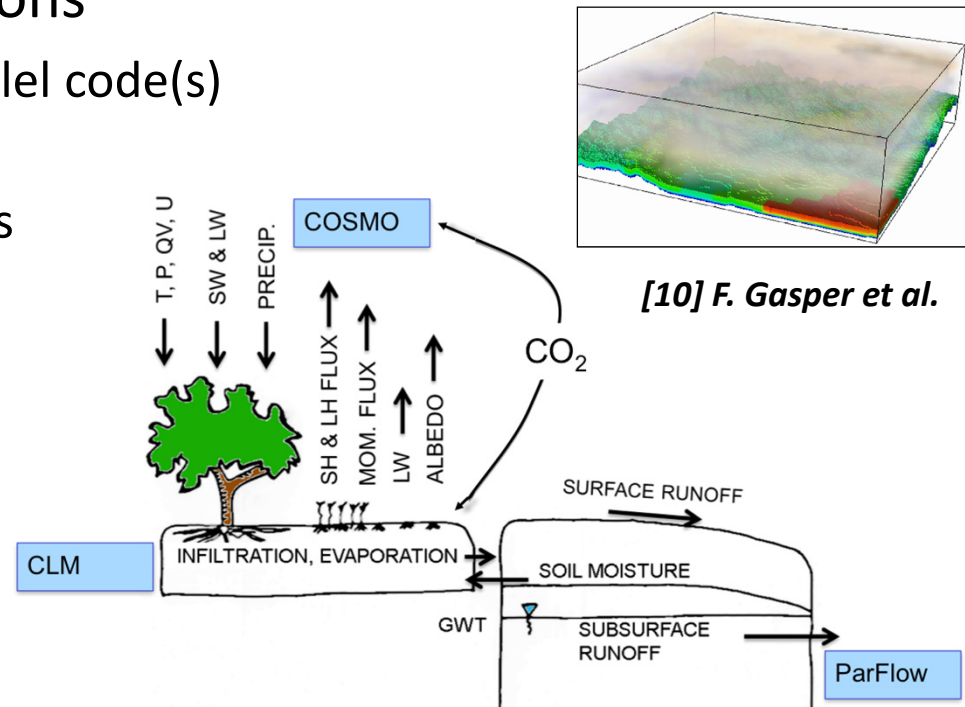
during integration step each processor updates the values of its local subdomain



[9] *COSMO Web page*

# Terrestrial Systems – Coupling Different Parallel Libraries (1)

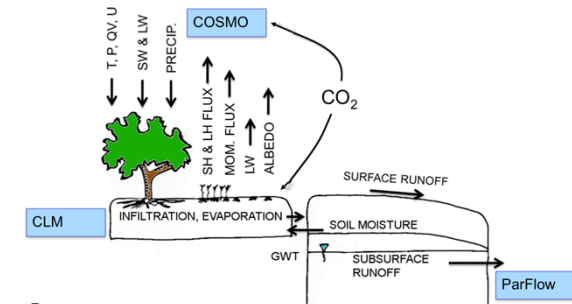
- **Scientific case:** understanding water cycle processes and variability across scales including climate and land use impacts
  - Computational challenge: earth system models at **regional scale**
- Terrestrial systems simulations
  - E.g. TerrSysMP coupled parallel code(s)
  - Many processes are still **poorly reproduced** by models
  - **Overcome isolated research** and simulation for specific elements in earth systems
  - Full integrated **groundwater-vegetation-atmosphere** simulation algorithms



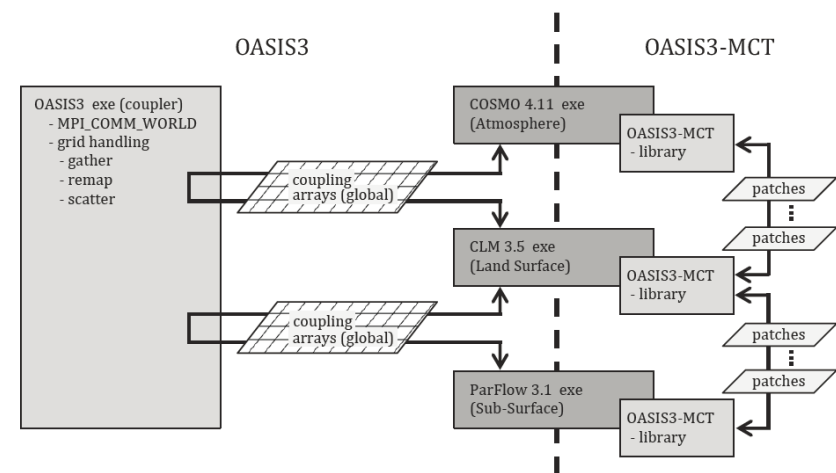
- **Coupled codes execute n different parallel application codes together to simulate one ecosystem**

# Terrestrial Systems – Coupling Different Parallel Libraries (2)

- Requires a **coupling technique** running on a HPC machine
  - Example: **OASIS3 coupler** for ParFlow, CLM & COSMO
  - 1+3 parallel applications together referred to as **‘TerrSysMP parallel coupled application’**
  - OASIS3 is a **separate executable** that manages data exchange between others
  - Coupling data arrays are **repartitioned to the full domain** by OASIS
  - OASIS3-MCT library** is part of each component model
  - Coupling arrays only consist of the **local fraction** of full domain
  - Routed by OASIS** to the destination processor



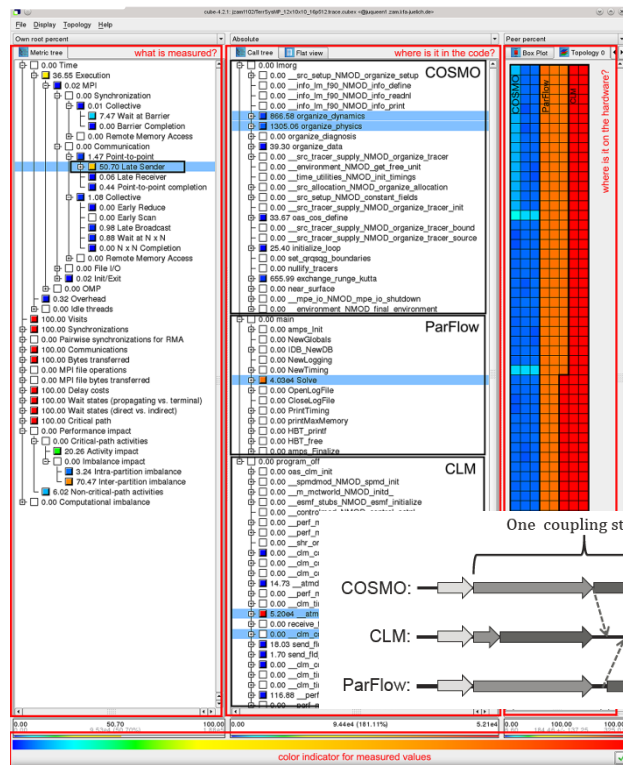
[10] F. Gasper et al.



**Coupled codes require another separate executable that is a coupler exchanging global data**

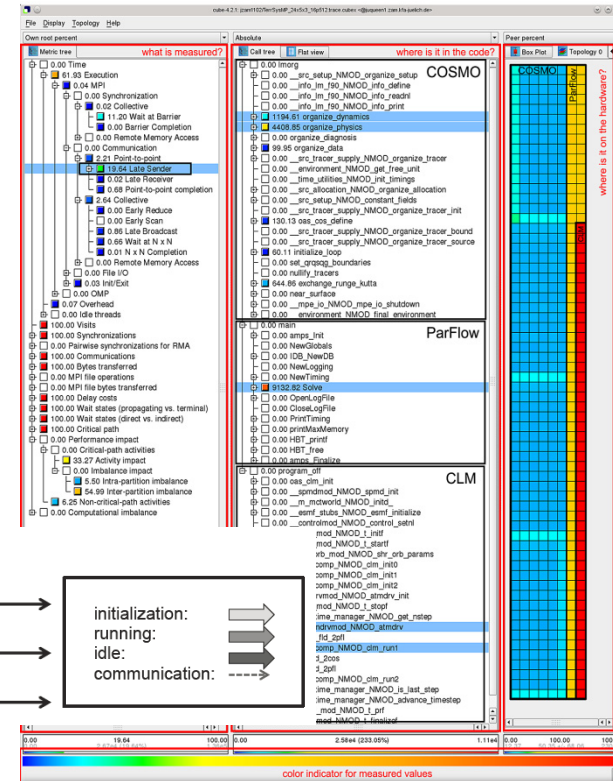
# Terrestrial Systems – Coupling Different Parallel Libraries (3)

- Performance optimization required (cf. Lecture 9) [10] F. Gasper et al.
  - Using performance analysis tool SCALASCA
  - Resources are distributed according to load (better load balance)
  - LateSender wait state is significantly reduced



analysing & tuning

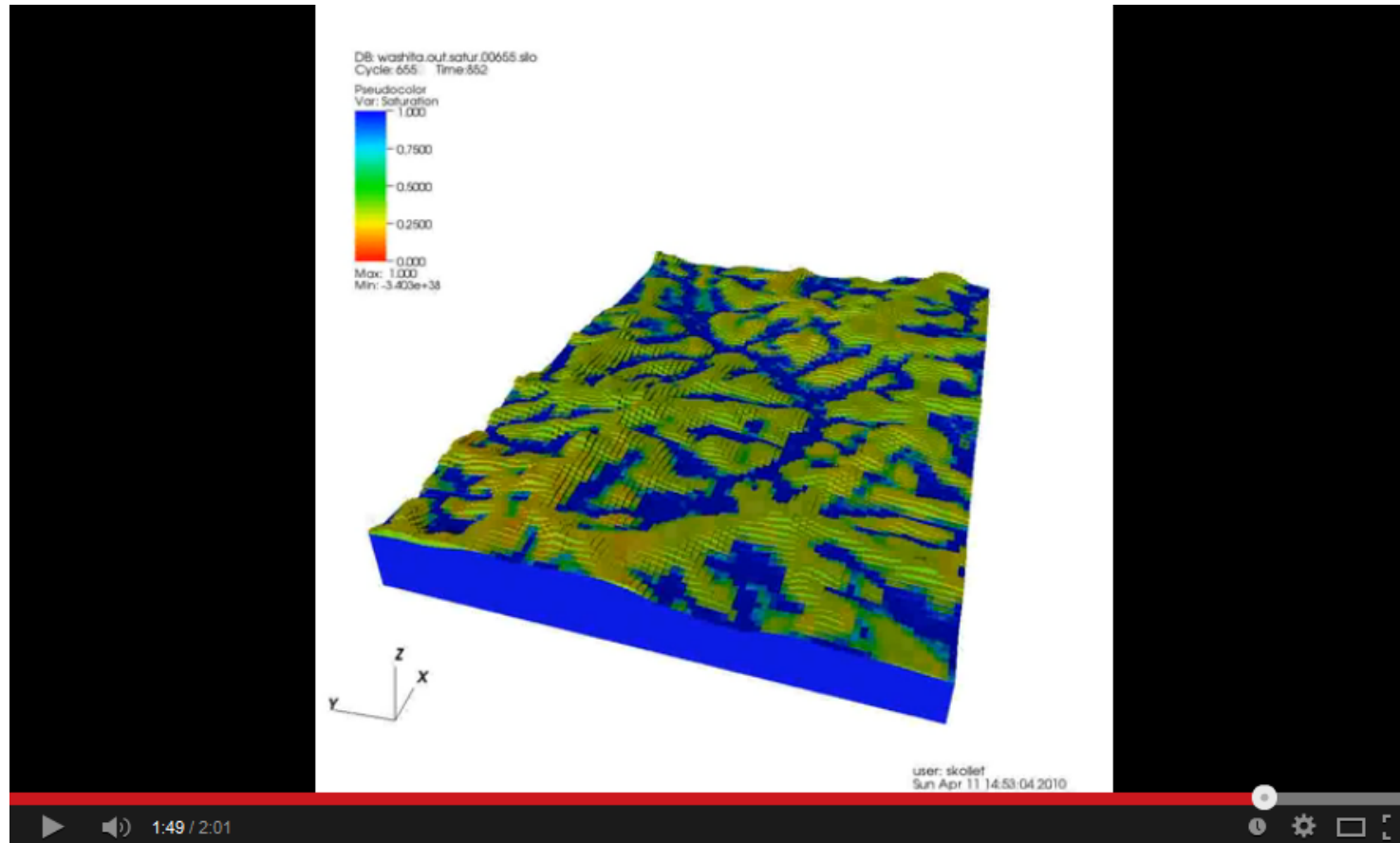
→



Before:  
 Processor distribution  
 192 COSMO  
 160 ParFlow  
 160 CLM

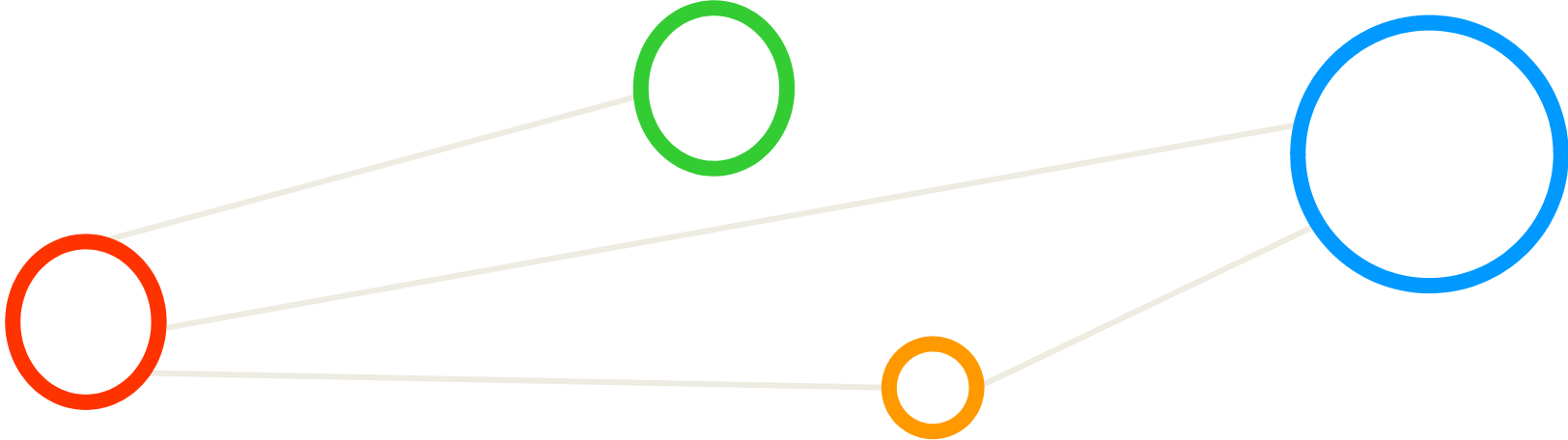
After:  
 Processor distribution  
 384 COSMO  
 80 ParFlow  
 48 CLM

# [Video] Terrestrial Systems with ParFlow coupled with CLM



**[11] ParFlow coupled with CLM**

# Climate

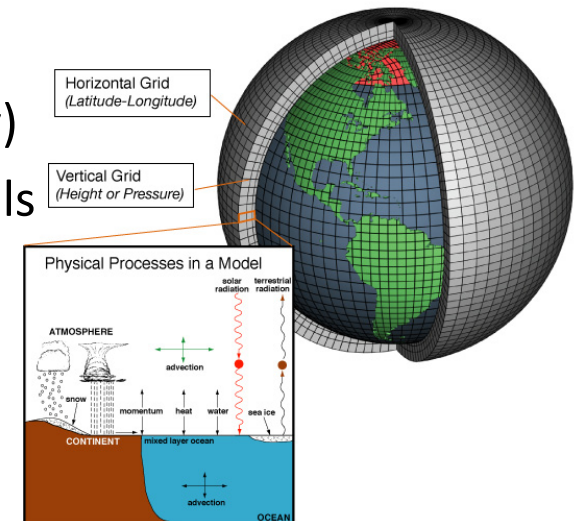


# Climate – Numerical Weather Prediction & Forecast

- Numerical Weather Prediction (NWP) uses mathematical models of the atmosphere and oceans to predict the weather based on current weather observations (e.g. weather satellites) as inputs.
- Performing complex calculations necessary for NWP requires supercomputers (limit ~6 days)
- NWP belongs to the field of numerical methods that obtain approximate solutions to problems

*modified from [12] Wikipedia on 'Numerical Weather Prediction'*

- Application areas
  - Global and regional **short-term weather forecast** models in operations
  - Perform **long-term climate prediction** research (e.g. climate change)
- NWP model characteristics
  - Use **ordinary/partial differential equations (PDEs)** (i.e. use laws of physics, fluids, motion, chemistry)
  - **Domain decomposition (cf. Lecture 2):** 3D grid cells
  - **Computing/cell:** winds, heat transfer, solar radiation, relative humidity & surface hydrology
  - **Interactions with neighboring cells:** used to calculate atmospheric properties **over time**



# Climate – PDEs in Atmospheric Research (1)

## ■ HPC Atmospheric Models

- Simulations produce meteorological information for given locations
- Different ‘temporal resolutions/scales’: future times, days to decades
- Different ‘spatial resolutions/scales’: meters to kilometers
- Use primitive equations to enable model evolution over space and time

■ Primitive equations are a set of nonlinear differential equations that are used to approximate global atmospheric flow in atmospheric models and predict/simulate future states of atmospheres

*modified from [13] Wikipedia on ‘Primitive Equations’*

## ■ Set of Primitive Equations

1. **Conservation of momentum:** Describe hydrodynamical flow on the surface of a sphere (e.g. vertical motion smaller than horizontal motion)
2. **Thermal energy equation:** Overall temperature of the modelled system in relation to heat sources and sinks
3. **Continuity equation:** Describe the conservation of mass



# Climate – PDEs in Atmospheric Research (2)

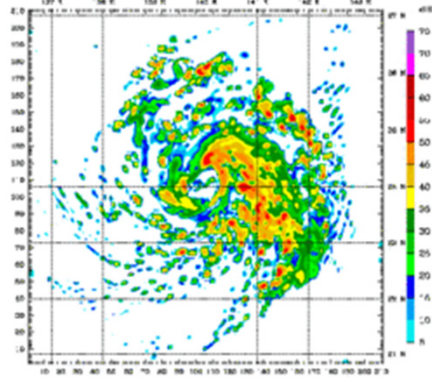
- HPC Model **evolution over space and time**
  - Based on primitive equations (alongside e.g. **gas laws**)
  - Simulations change of density, pressure, potential temperature scalar fields, air velocity (aka wind) vector fields of the atmosphere over time
- **Computational challenges**
  - Nonlinear PDEs are **impossible to solve exactly** through analytical methods
  - Idea is to obtain approximate solutions with **numerical methods**
- **Simulation over time**
  - Initialization of equations based on analysis data or research question
  - Rates of changes determined via a time increment known as **'time step'**
  - **Approach is repeated** until solution reaches the desired forecast time

- **Simulations over time need to maintain 'numerical stability': the length of the time step chosen within the model is related to the distance between the points on the computational grid**

*modified from [12] Wikipedia on 'Numerical Weather Prediction'*

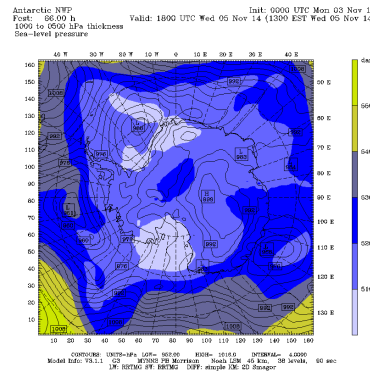
# Climate – WRF Model Parallel Application – Examples

[14] Wikipedia on 'WRF'



WRF model output showing simulated radar reflectivity (rBZ) for Typhon Mawar (3.3km grid)

[15] Polar WRF

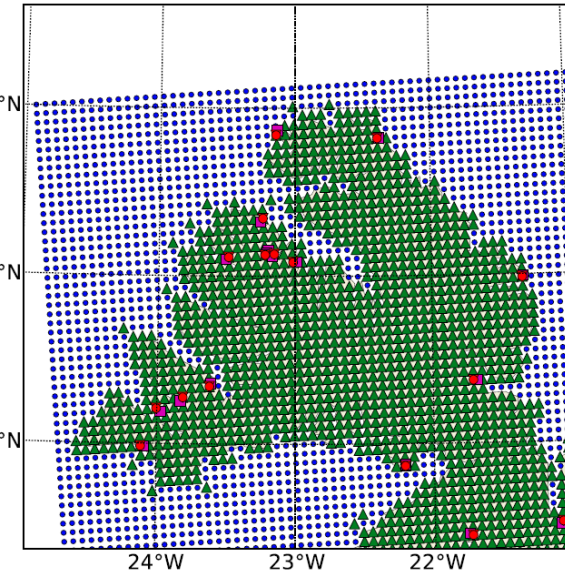


WRF polar model output showing 1000 – 500 hPa thickness & sea level pressure

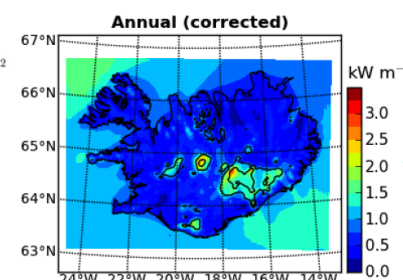
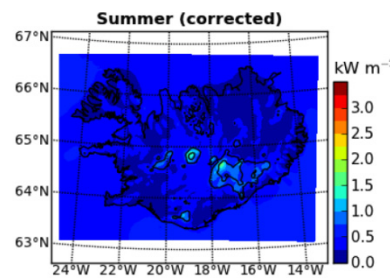
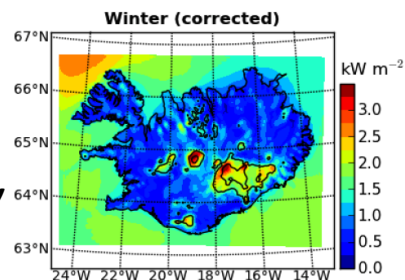
[16] Evaluation of WRF Mesoscale model



Align data measurement stations in Iceland with WRF model (closest land gridpoints as red dots)



[17] Iceland wind energy potential study, 2013



WRF model output showing wind power density across Iceland at 50 mAGL

- Software package Weather Research and Forecasting (WRF) includes parallelization techniques and enables a wide range of meteorological applications across scales (meters – 1000 of KMs)

# Climate – WRF Model Parallel Application – Software

- The WRF model is a NWP system that enables the simulation and prediction of the atmosphere
- It is a scalable parallel HPC simulation for distributed-memory & shared-memory systems

[18] WRF model Webpage

- Weather Research and Forecasting (WRF) model

- Takes advantage of PDEs (and parallel solvers)
- Maintained and support as a community model
- Plug-compatible modules for extensions
- Research advances have direct path to operations
- Numerous physics options (link with the broader HPC modeling community) (e.g. air quality modeling)



code used for daily weather forecasts by MetOffices worldwide as service to tax payers

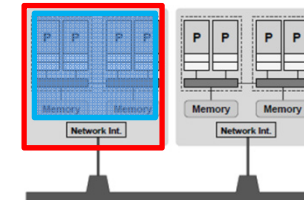
tax payers pay some scientists to better the WRF model  
→ ROI / impact over years

- Selected software package features

- Available as open-source tool implementing parallelization techniques
- Implements a modular & hierarchical design
- Supports a model coupling infrastructure & NetCDF data format support
- Enables integration into bigger earth system model frameworks

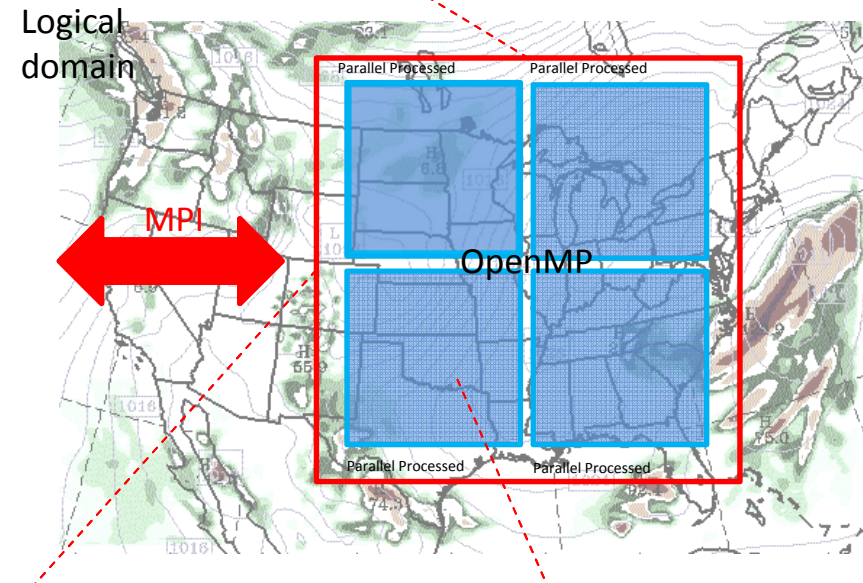
# Climate – WRF Model Parallel Application – Parallelization (1)

- Parallel simulation sciences
  - E.g. reflecting real data obtained from observations, analyses, etc.
  - E.g. enable idealized atmospheric conditions
- Approach
  - Implements ‘hybrid programming’ (cf. Lecture 7)
  - Use of ‘domain decomposition’ (cf. Lecture 2) dividing work
  - Model domains are decomposed for parallelism on two-levels using ‘patches’ and ‘tiles’



(patch: section of model domain allocated to a distributed memory node)

(mediation layer solver or physics driver)



(one patch is divided into multiple tiles)

(tile: section of a patch allocated to a shared-memory processor within a node)

*modified from [19] WRF – Code and Parallel Computing*

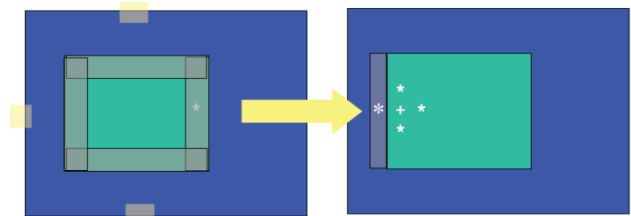
# Climate – WRF Model Parallel Application – Parallelization (2)

- Usage for ‘halo’ (cf. Lecture 7)
  - Code example based on Fortran
  - Horizontal data dependencies
  - E.g.  $i+1$ ,  $i-1$ , etc.: indexed operands may lie in the patch of a neighboring processor
  - Problem: neighbor’s updates to such an element of the array is not accessible on this processor

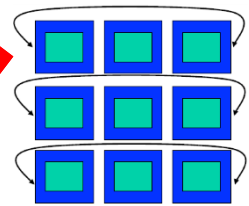
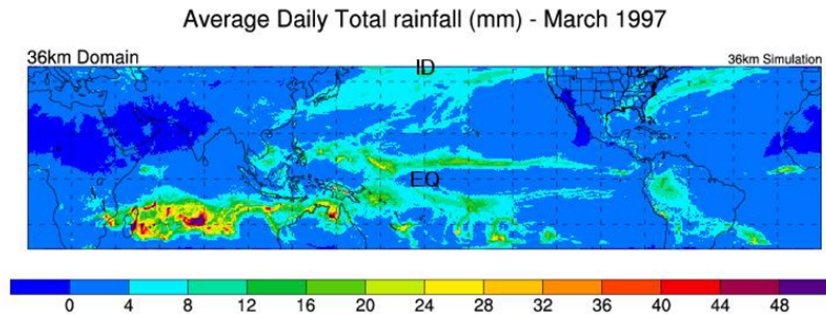
```

(module_diffusion.F)

SUBROUTINE horizontal_diffusion_s (tendency, rr, var, . . .
. . .
DO j = jts,jte
DO k = kts,ktf
DO i = its,ite
  mrdx=msft(i,j)*rdx
  mrdy=msft(i,j)*rdy
  tendency(i,k,j)=tendency(i,k,j)-
    (mrdx*0.5*((rr(i+1,k,j)+rr(i,k,j))*H1(i+1,k,j)-
      (rr(i-1,k,j)+rr(i,k,j))*H1(i,k,j))+
    mrdy*0.5*((rr(i,k,j+1)+rr(i,k,j))*H2(i,k,j+1)-
      (rr(i,k,j-1)+rr(i,k,j))*H2(i,k,j)))-
    msft(i,j)*(H1avg(i,k+1,j)-H1avg(i,k,j)+
      H2avg(i,k+1,j)-H2avg(i,k,j)
      )/dzeta(k)
. . .
ENDDO
ENDDO
ENDDO
. . .
    
```



(halo updates: get values from memory of left processor to memory of right neighbour processor)

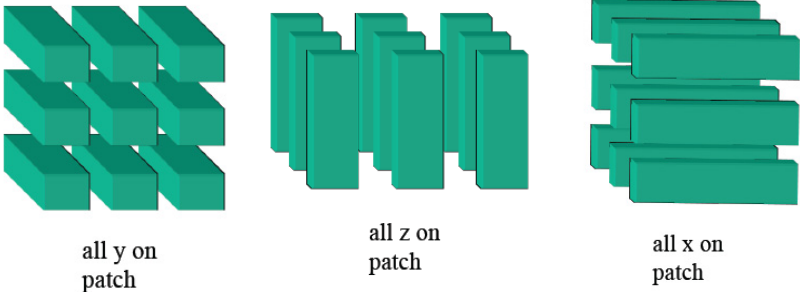


(Periodic boundary updates use interprocess communication)

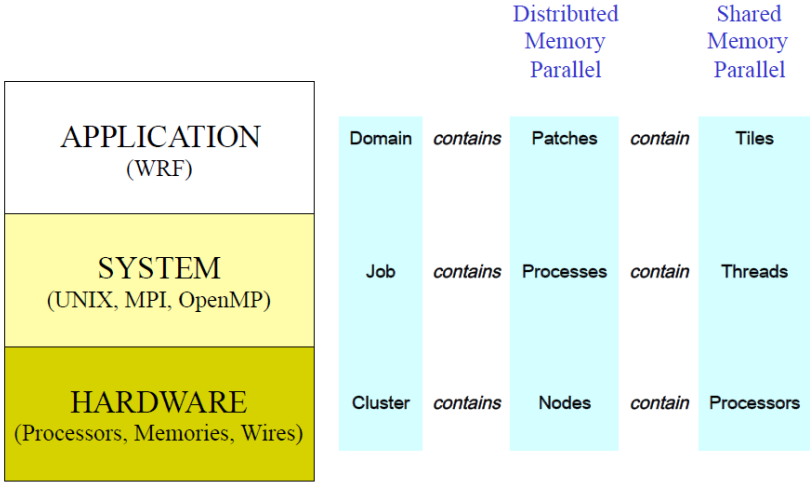
modified from [19] WRF – Code and Parallel Computing

# Climate – WRF Model Parallel Application – Parallelization (3)

- Usage for **transposes**
  - Different **parallel transposes** are supported
  - Take advantages of MPI



- Overview of parallelization
  - HPC terminology** vs. application **domain-specific terminology**
  - Evolved differently in time

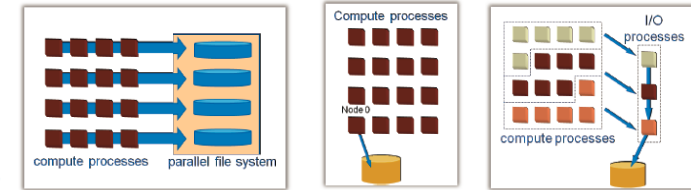


[19] WRF – Code and Parallel Computing

One of the most common misunderstandings between the technical HPC community and the application domain-specific communities (e.g. climate) are wrongly interpreted terminologies

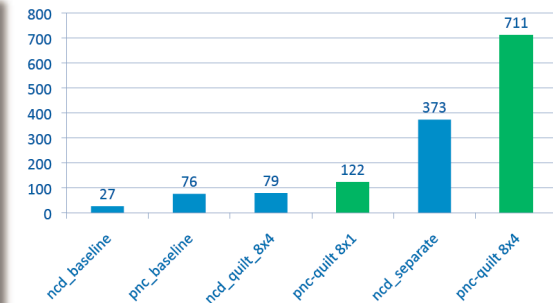
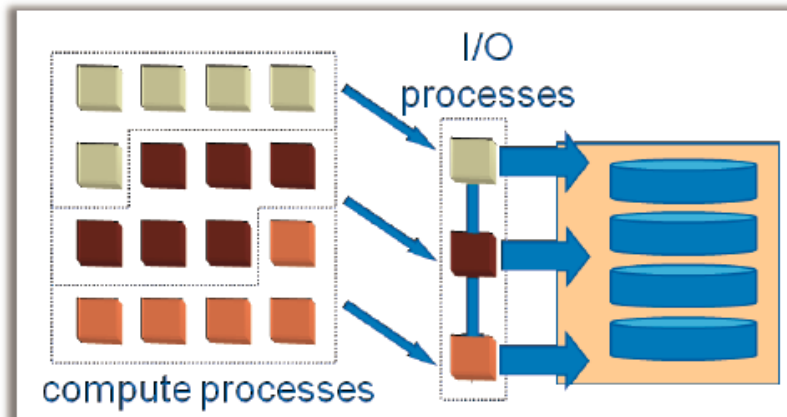
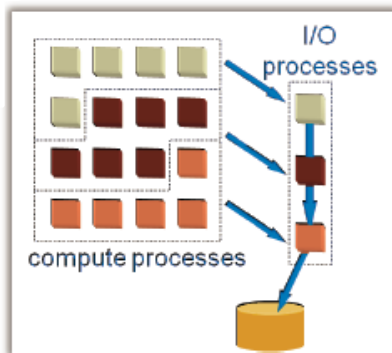
# Climate – WRF Model Parallel Application – pNetCDF

- Need for Parallel I/O (cf. Lecture 4)
  - WRF is output-bound ('writes costs much')
- Use Serial & parallel NetCDF (cf. Lecture 4)
  - Provides an I/O layer implemented with parallel NetCDF (pNetCDF)
  - I/O performance gain is considerable against using not pNetCDF



(different options that do not scale)

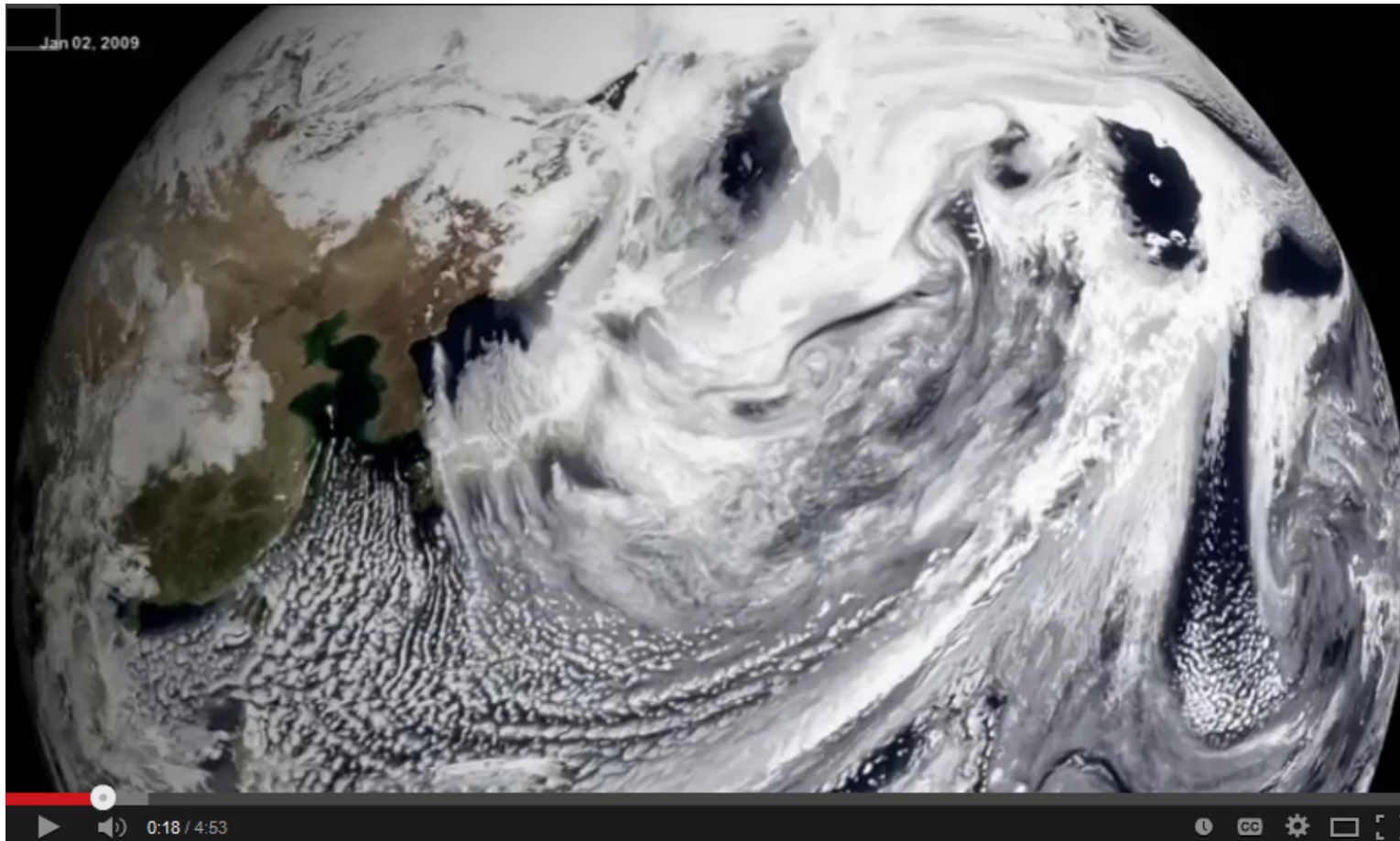
Serial NetCDF collected and written by gangs of MPI tasks (quilting)  
 Parallel NetCDF written to single files by all MPI tasks in a gang



[20] Opportunities for WRF Model Acceleration

Parallel NetCDF can be used to significantly improve I/O output performance of WRF codes

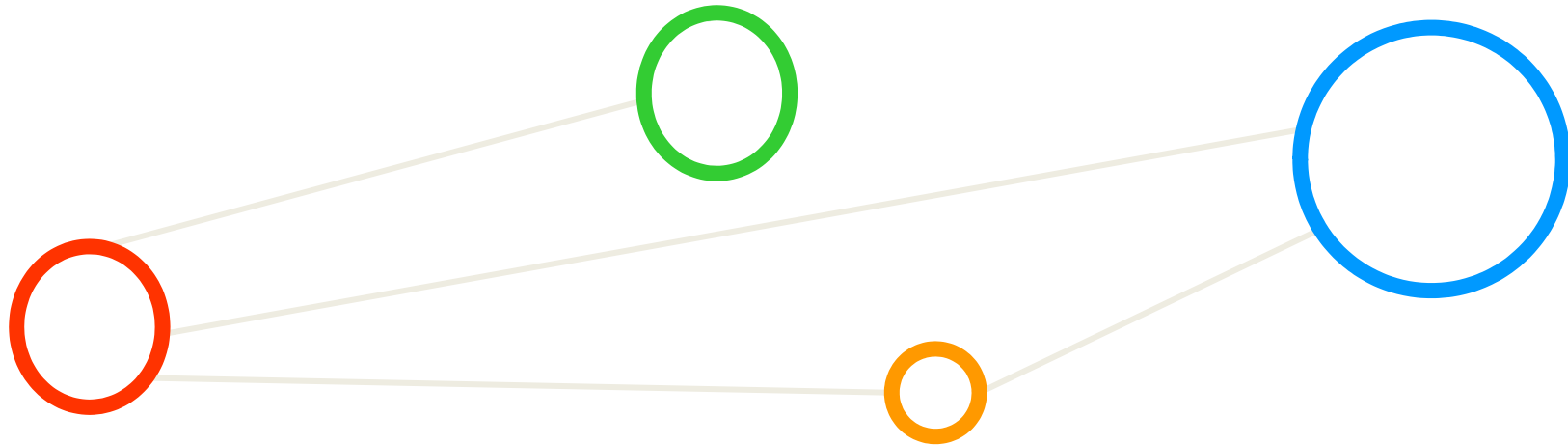
# [Video] Climate Modeling with Supercomputers



*[21] Climate modelling with Supercomputers*



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